

Welcome to Maple, eh! The very first thing we want to do before we start working is to type:

restart

This clears the memory buffer of any existing variable or function definitions.

Functions:

To define a function $f(x) = \sin(x)$, say, type

$$f := x \rightarrow \sin(x) \qquad x \rightarrow \sin(x) \qquad (1)$$

You can then call this function using a variable as input,

$$f(x) \qquad \sin(x) \qquad (2)$$

or you can evaluate it as an actual number as input:

$$f\left(\frac{\text{Pi}}{4}\right) \qquad \frac{1}{2} \sqrt{2} \qquad (3)$$

Maple likes to give us results symbolically, not numerically, so in order to see what that number is, type

$$\text{evalf}(\%) \qquad 0.7071067810 \qquad (4)$$

Here, *evalf*() means "evaluate function", and the % means "last line calculated". We can alternatively combine the two steps:

$$\text{evalf}\left(f\left(\frac{\text{Pi}}{4}\right)\right) \qquad 0.7071067810 \qquad (5)$$

Note that we can choose (almost) any name we want for our functions, as long as they don't conflict with pre-defined variable or function names. So, instead of the lame $f(x)$, we could instead have called it *myfirstfunction*:

$$\text{myfirstfunction} := x \rightarrow \sin(x) \qquad x \rightarrow \sin(x) \qquad (6)$$

which we can invoke accordingly:

$$\text{myfirstfunction}(x) \qquad \sin(x) \qquad (7)$$

Functions can be multivariate, and we'll frequently need to define these. For example,

$$f2 := (x, a) \rightarrow a \cdot \sin(x)$$

$$(x, a) \rightarrow a \sin(x) \quad (8)$$

is now a sine function whose amplitude we can vary as input:

$$f_2(x, a) \quad a \sin(x) \quad (9)$$

$$f_2\left(\frac{\text{Pi}}{4}, 1\right) \quad \frac{1}{2} \sqrt{2} \quad (10)$$

$$f_2\left(\frac{\text{Pi}}{4}, 2\right) \quad \sqrt{2} \quad (11)$$

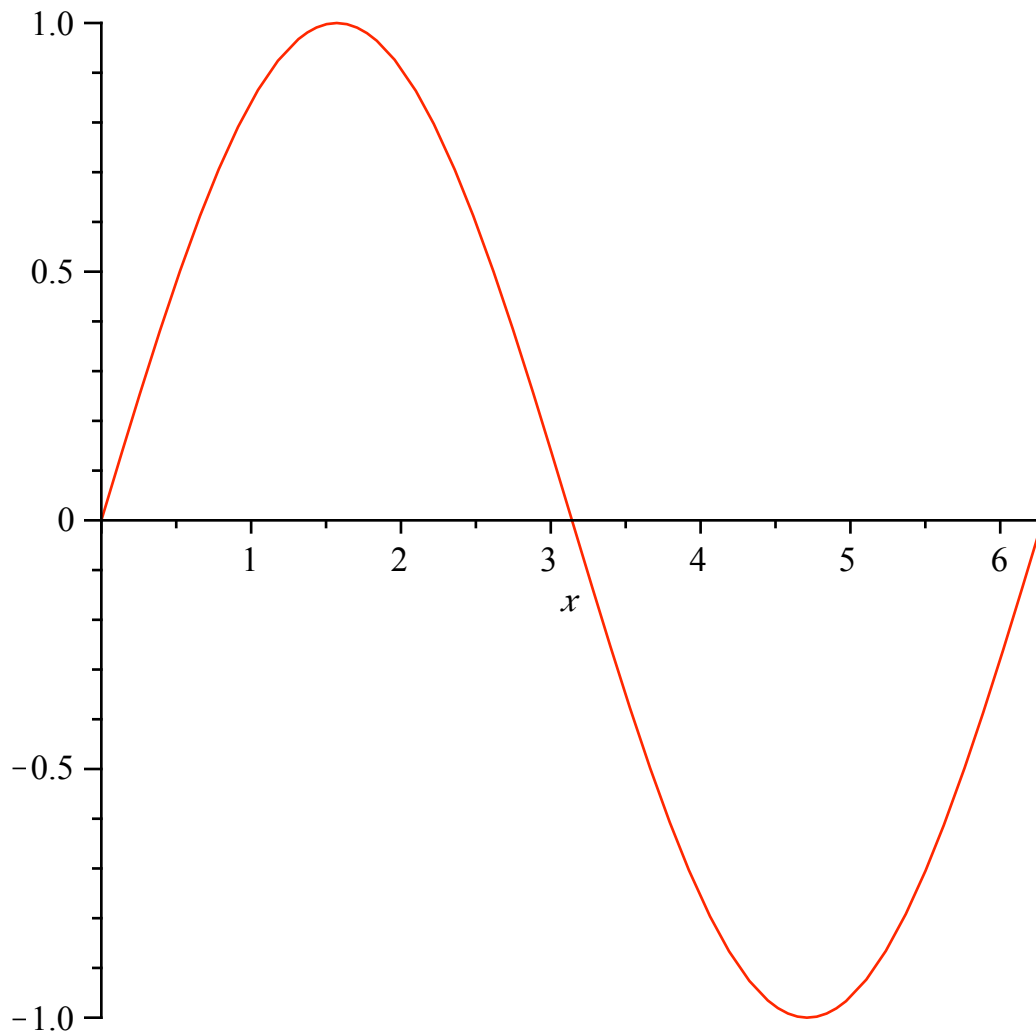
and so on. There's no limit to how many input variables you want to define.

Plotting

After we define our functions, we will also want to plot them. Plotting is a fairly simple procedure, but you have to watch your syntax.

Suppose we want to plot $f(x)$ as defined above. The only variable is x , so we would type

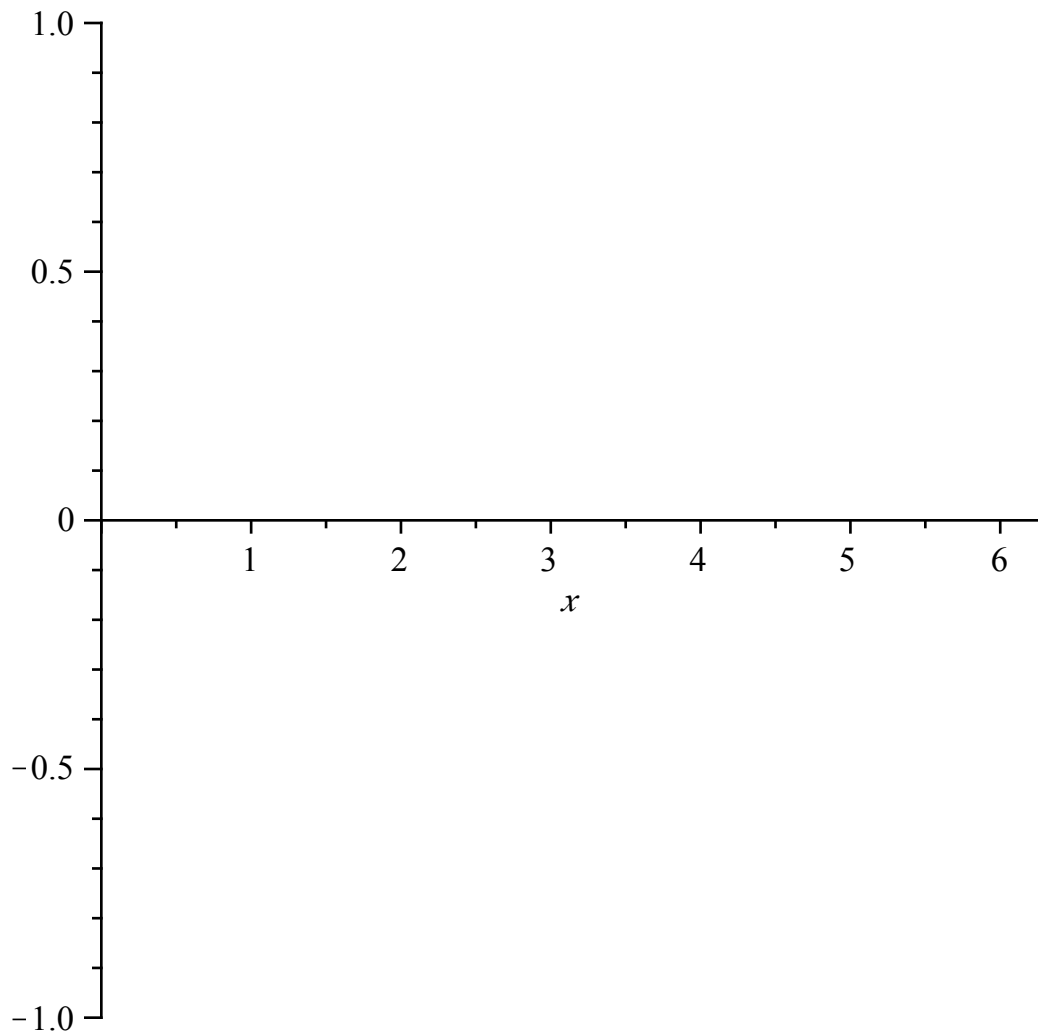
```
plot(f(x), x=0..2 * Pi)
```



That is, of course, what we expect to see! We can vary the range to whatever we want.

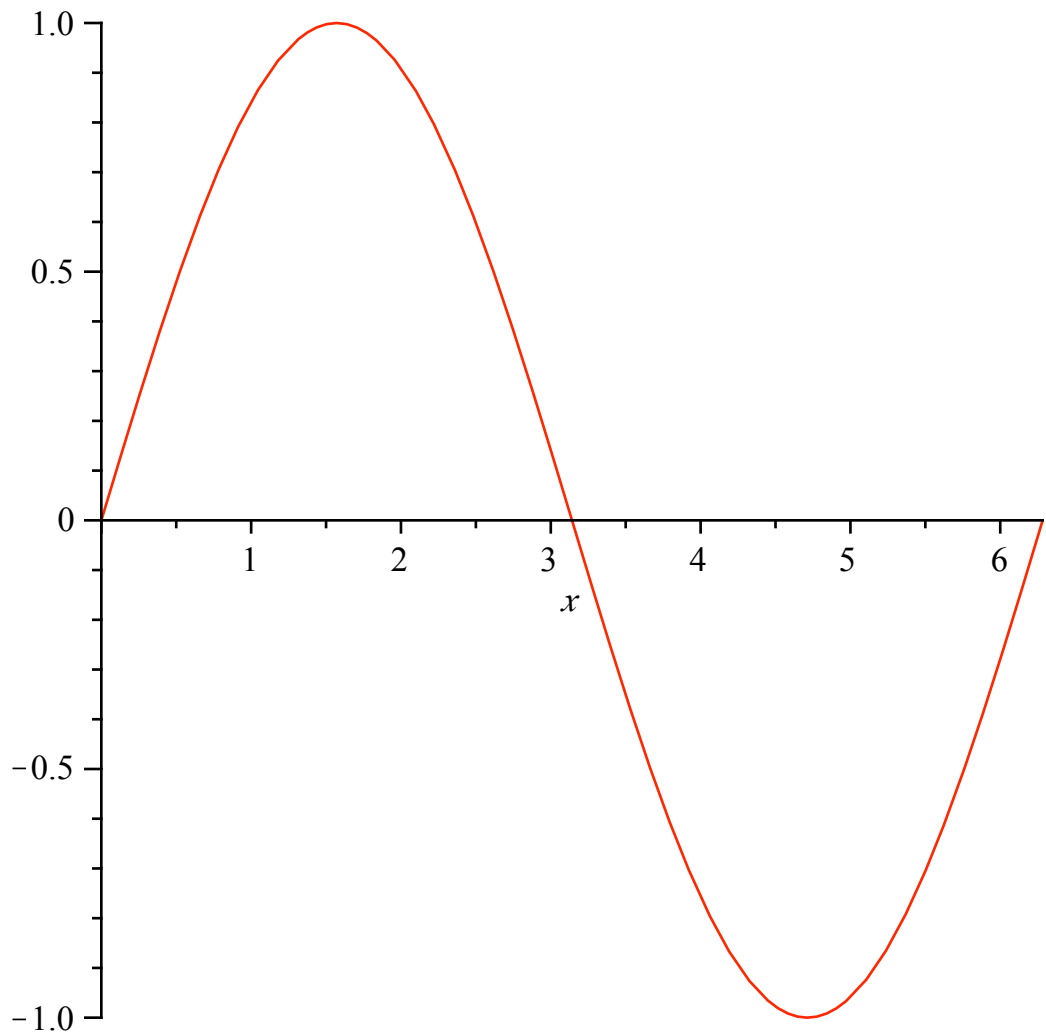
To plot our second function of two variables, let's type:

```
plot(f2(x, a), x=0 ..2 Pi)
```

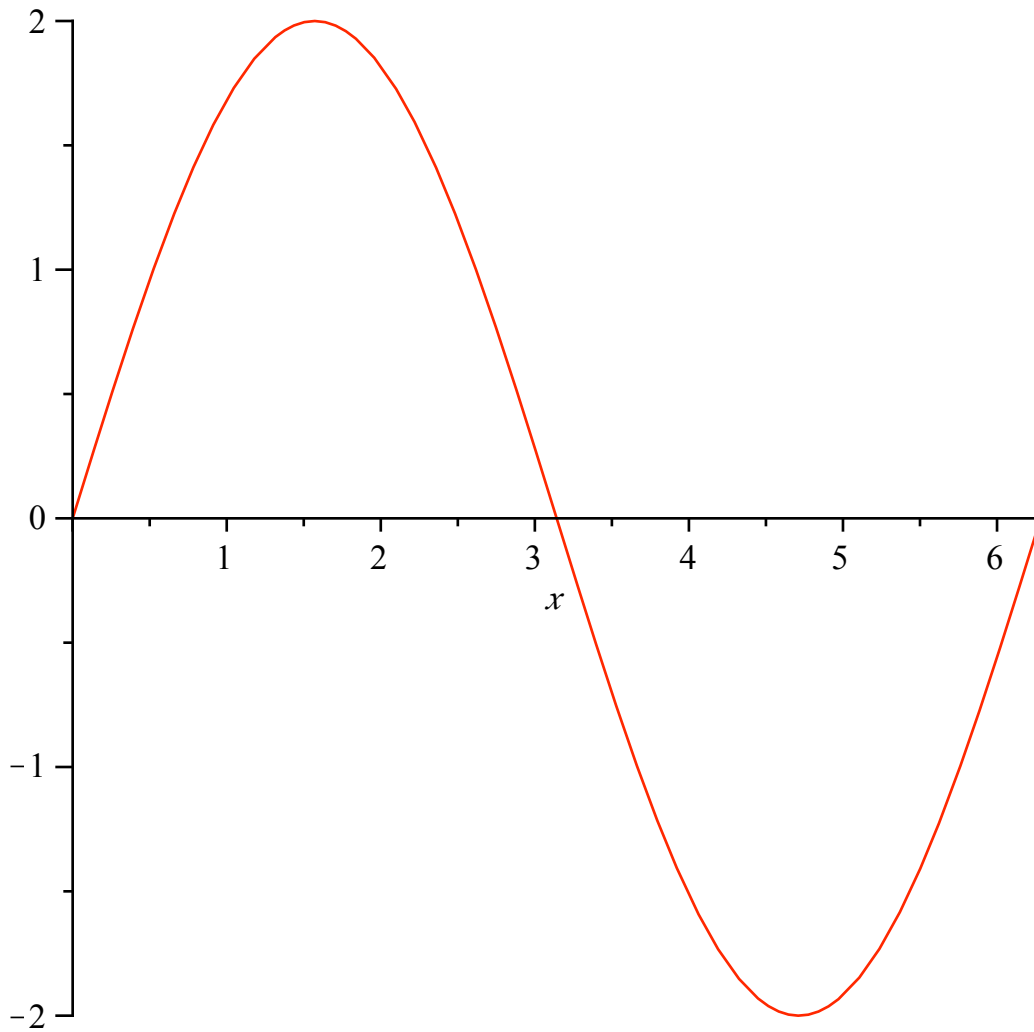


Uh oh! Why didn't it show anything? Duh! We forgot to set a value for α . Let's try again:

```
plot(f2(x, 1), x=0 ..2 Pi)
```



plot(f2(x, 2), x=0 ..2 Pi)



Much better!

Integrating and Differentiating

The other important thing we'll need to do is calculus. To differentiate a function, type

$$\text{diff}(f(x), x) \qquad \qquad \qquad \cos(x) \qquad \qquad \qquad (12)$$

To perform an indefinite integrate, type

$$\text{int}(f(x), x) \qquad \qquad \qquad -\cos(x) \qquad \qquad \qquad (13)$$

and for a definite integral, we need to specify bounds (but they need not be numerical):

$$\text{int}(f(x), x=0..Pi) \qquad \qquad \qquad 2 \qquad \qquad \qquad (14)$$

$$\text{int}\left(f(x), x=0..\frac{b}{2}\right)$$

$$1 - \cos\left(\frac{1}{2} b\right) \quad (15)$$

This works with multivariate functions as well, and this time you don't need to define the value of any other variable (but you can if you want):

$$\text{diff}(f2(x, a), x) \quad a \cos(x) \quad (16)$$

$$\text{diff}(f2(x, 2), x) \quad 2 \cos(x) \quad (17)$$

$$\text{int}(f2(x, a), x) \quad -a \cos(x) \quad (18)$$

and so on.

We can perform higher-order derivatives. Here's the second derivative:

$$\text{diff}(f(x), x^2) \quad -\sin(x) \quad (19)$$

$$\text{diff}(f2(x, a), x^2) \quad -a \sin(x) \quad (20)$$

and we can also perform multidimensional integration:

$$\text{int}(\text{int}(f2(x, a), x=0..b), a=-1..c) \quad \frac{1}{2} (1 - \cos(b)) (c^2 - 1) \quad (21)$$

The possibilities are endless, but that's enough to start you out on the road.